







Office of

Science



「偏極、 CME、 CVE」



筑波大学 University of Tsukuba

WAYNE STATE UNIVERSITY

チュートリアル研究会「高エネルギー原子核衝突の物理」 2019年8月19-21日,理化学研究所



Strong magnetic field

 $B \sim 10^{13} {
m T}$ $(eB \sim \mathrm{MeV}^2 \ (\tau = 0.2 \ \mathrm{fm}))$

D. Kharzeev, L. McLerran, and H. Warringa, Nucl.Phys.A803, 227 (2008) McLerran and Skokov, Nucl. Phys. A929, 184 (2014)

> \rightarrow Chiral magnetic effect Chiral magnetic wave Particle polarization

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spectators

→Chiral vortical effect Particle polarization



Chiral Magnetic Effect (CME)

Magnetic field massless quarks chirality imbalance ++

spin alignment *(opposite direction* for opposite sign)



Induction of electric current along the magnetic field is called Chiral Magnetic Effect (CME)

詳細は山本さんの講演参照

D. Kharzeev, R. Pisarski, M. Tytgat, PRL81, 512 (1998) D. Kharzeev, PPNP75(2014)133-151





Experimental observable of CME



* Magnetic field direction is perpendicular to the reaction plane in heavy-ion collisions

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"Gamma correlator" sensitive to the charge separation S.Voloshin PRC70, 057901 (2004)

$$\gamma_{\alpha\beta} = \left\langle \cos(\phi_{\alpha} + \phi_{\beta} - 2\Psi_{RP}) \right\rangle$$
$$\Delta\gamma = \gamma_{+-} - \gamma_{\pm\pm}$$

π/2

RP

e.g. extreme case of charge separation

$$\gamma_{\pm} = \langle \cos(\pi/2 - \pi/2) \rangle = 1$$

$$\gamma_{\pm\pm} = \langle \cos(\pi/2 + \pi/2) \rangle = -1$$

$$\Delta\gamma = 2$$



y correlator in anomalous hydrodynamics



Y. Hirono, T. Hirano, and D. Kharzeev, arXiv:1412.0311



Anomalous y correlator is indeed sensitive to CME!



y-correlator at RHIC and the LHC



Charge separation was observed at RHIC and the LHC! The difference between charge combinations ($\Delta\gamma$) decreases in lower energies.

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D. Kharzeev, J. Liao, S. Voloshin, and G. Wang, PPNP88(2016)1-28 STAR, PRL113, 052302 (2014) ALICE, PRL110, 021301 (2013)

Known background





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- S.Voloshin PRC70, 057901 (2004)
- S. Schlichting and S. Pratt, PRC83, 014913 (2011)
- A. Bzdak, V. Koch, and J. Liao, PRC83, 014905 (2011)

e.g. resonance contributes to $\Delta \gamma$, stronger collimation in in-plane

e.g. back-to-back jets, important at low multiplicity, n gap wouldn't help

011) 5 (2011)

At Small system



CME is not expected in p(d)+A collisions. Background (back-to-back jets) would be dominant in low multiplicity events.

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Using event shape engin

Event shape engineering (ESE) J. Schukraft, A. Timmins, and S. Voloshin, PLB719 (2013) 394 Select larger/smaller v₂ events, likely selecting initial eccentricity



Estimate the CME contribution comparing the slopes with models - assuming the background is linearly proportional to v_2 - model-dependent estimate of magnetic field at $\tau=0.2$ fm/c



ALICE, PLB777(2018)151



Possible CME contribution



CMS, PRC97, 044912 (2018) ALICE, PLB777(2018)151 **STAR, QM2018**







Current observables at a glance

Slide from S. Voloshin @chirality workshop 2019



- A lot of idea/observables but need to make their assumptions clear
- Results of isobaric collisions will come soon (see outlook slide)

Chiral Vortical Effect (CVE)

Similar to CME, system rotation leads to vector and axial current along ω



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詳細は山本さんの講演参照

D. Kharzeev and D. Son, PRL106.062301 (2011) D. Kharzeev et al., PPNP88(2016)1-28

$$J_E^{\text{CME}} \sim \frac{2}{3}(N_f = 3)$$
 or $\frac{5}{9}(N_f = 2)$
 $J_B^{\text{CME}} = 0(N_f = 3)$ or $\sim \frac{1}{9}(N_f = 3)$

$$J_E^{\text{CVE}} = 0(N_f = 3) \text{ or } \sim \frac{1}{3}(N_f = J_B^{\text{CVE}} \sim 1(N_f = 3) \text{ or } \sim \frac{2}{3}(N_f = 2)$$

Q(u, d, s) = (+2/3, -1/3, -1/3)B(u, d, s) = (1/3, 1/3, 1/3)

Spin polarization by vorticity is "charge-blind". CVE mostly contributes to baryon current.











YEvent Plane Reconstruction: arg Big hy on degage proprint and all



Vorticity in HIC



In non-central collisions, the initial collective longitudinal flow velocity depends on x.

$$\omega_y = \frac{1}{2} (\nabla \times v)_y \approx -\frac{1}{2} \frac{\partial v_z}{\partial x}$$

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Global polarization



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- Z.-T. Liang and X.-N. Wang, PRL94, 102301 (2005)

- S. Voloshin, nucl-th/0410089 (2004)

Non-zero angular momentum transfers
 to the spin degrees of freedom

• Particles' and anti-particles' spins are aligned with angular momentum, *L*

•Magnetic field align particle's spin

 Particles' and antiparticles' spins are aligned oppositely along *B* due to the opposite sign of magnetic moment



Rotation vs. Polarization

Barnett effect: rotation→polarization

Magnetization of an uncharged body when spun on its axis S. Barnett, Phys. Rev. 6, 239 (1915)



figure: M. Matsuo et al., Front. Phys., 30 (2015)

$$M = \frac{\chi \omega}{\gamma}$$

 χ : magnetic susceptibility γ : gyromagnetic ratio

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<u>Einstein-de-Haas effect:</u> polarization→rotation



"the only experiment by Einstein"

Rotation of a ferromagnet under change in the direction/strength of magnetic-field to conserve the total angular momentum.

$$\vec{J} = \vec{L} + \vec{S}$$

A.Einstein, W. J. de Haas,

B.Koninklijke Akademie van Wetenschappen te Amsterdam, C.Proceedings, 18 I, 696-711 (1915)

How to measure the global polarization?

Parity-violating decay of hyperons

Daughter baryon is preferentially emitted in the direction of hyperon's spin (opposite for anti-particle)

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_{\rm H} \mathbf{P}_{\rm H} \cdot \mathbf{p}_{\mathbf{p}}^*)$$

 P_{H} : Λ polarization $\alpha_{\rm H}$: Λ decay parameter $(\alpha_{\wedge} = -\alpha_{\bar{\wedge}} = 0.642 \pm 0.013)$



C. Patrignani et al. (PDG), Chin. Phys. C 40, 100001 (2016)

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Projection onto the transverse plane

Angular momentum direction can be determined by spectator deflection (spectators deflect outwards) - S. Voloshin and TN, PRC94.021901(R)(2016)

> Ψ_1 : azimuthal angle of b ϕ_{p}^{*} : ϕ of daughter proton in Λ rest frame STAR, PRC76, 024915 (2007)







nature

THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE

First observation of fluid vortices formed by heavyion collisions

SUBRES IN RUS

CLIMATE CHANGE

PARIS AGREEMENT Time for nations to match words with deeds PAGE 25 SUMMER SELECTION Recommended reading for the holiday season PAGE 28

BOOKS

STEM CELLS

YOUTHFUL SECRETS How the hypothalamus helps to control the ageing process PAGE 52

First observation of fluid vortices formed by HIC

Discover Magazine, 2017





#38



The Fastest Fluid by Sylvia Morrow

Superhot material spins at an incredible rate.

... AND MORE!

August 2017 Vol. 548, No. 7665

First observation of fluid vortices in HIC



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Positive polarization signal at lower energies! -- The most vortical fluid!

> $\omega = (P_{\Lambda} + P_{\bar{\Lambda}})k_BT/\hbar$ μ_{Λ} : Λ magnetic moment $\sim 0.02 \text{--} 0.09 \text{ fm}^{-1}$ T: temperature at thermal equilibrium $\sim 0.6\text{-}2.7 imes 10^{22} \mathrm{s}^{-1}$ (T=160 MeV)

- P_H looks to increase in lower energies

- Hint of the difference in P_H between Λ and anti- Λ -- Effect of the initial magnetic field? \rightarrow BESII

$$P_{\Lambda} \simeq \frac{1}{2} \frac{\omega}{T} + \frac{\mu_{\Lambda} B}{T}$$
$$P_{\bar{\Lambda}} \simeq \frac{1}{2} \frac{\omega}{T} - \frac{\mu_{\Lambda} B}{T}$$

Becattini, Karpenko, Lisa, Upsal, and Voloshin, PRC95.054902 (2017)





Vorticity we know

~10-5 s-1 Ocean surface vorticity ~10-4 s⁻¹ Jupiter's great red spot $\sim 10^{-1} \, \mathrm{s}^{-1}$ Core of supercell tornado Rotating, heated soap bubbles ~10² s⁻¹ Superfluid helium nano droplet ~10⁶ s⁻¹



Supercell in Oklahoma (2016) http://www.silverliningtours.com/tag/tornado/page/3/ T. Niida, HI Tutorial workshop, Riken







Great red spot of Jupiter

vortex aligned to x-ray beam in He droplets T. Muel et al., Scientific Report 3, 3455 (2013)

The most vortical fluid.

~10-5 s-1 Ocean surface vorticity $\sim 10^{-4} \text{ s}^{-1}$ Jupiter's great red spot $\sim 10^{-1} \text{ s}^{-1}$ Core of supercell tornado Rotating, heated soap bubbles ~10² s⁻¹ Superfluid helium nano droplet ~10⁶ s⁻¹ Matter in heavy ion collisions ~10²² s⁻¹



Supercell in Oklahoma (2016) http://www.silverliningtours.com/tag/tornado/page/3/ T. Niida, HI Tutorial workshop, Riken

T. Muel et al., Scientific Report 3

Ocean surface vorticity https://sos.noaa.gov/datasets/ocean-surface-vorticity/



vortex aligned to x-ray beam in He droplets T. Muel et al., Scientific Report 3, 3455 (2013)

Feed-down effect

from $\Sigma^* \rightarrow \Lambda \pi$, $\Sigma^0 \rightarrow \Lambda \gamma$, $\Xi \rightarrow \Lambda \pi$

 \Box Polarization of parent particle R is transferred to its daughter Λ

$$\begin{split} \mathbf{S}_{\Lambda}^{*} &= C \mathbf{S}_{R}^{*} \qquad \langle S_{y} \rangle \propto \frac{S(S+1)}{3} (\omega + \frac{\mu}{S} B) \\ \text{hi, Karpenko, Lisa, Upsal, and Voloshin, PRC95.054902 (2017)} \qquad \begin{array}{c} C_{\Lambda R} : \text{coefficient of spin transfer from parent} \\ S_{R} &: \text{parent particle's spin} \\ f_{\Lambda R} : \text{fraction of } \Lambda \text{ originating from parent } R \\ \mu_{R} &: \text{magnetic moment of particle } R \\ \end{array} \\ &= \begin{bmatrix} \frac{2}{3} \sum_{R} \left(f_{\Lambda R} C_{\Lambda R} - \frac{1}{3} f_{\Sigma^{0} R} C_{\Sigma^{0} R} \right) S_{R}(S_{R} + 1) & \frac{2}{3} \sum_{R} \left(f_{\Lambda R} C_{\Lambda R} - \frac{1}{3} f_{\Sigma^{0} R} C_{\Sigma^{0} R} \right) (S_{R} + 1) \mu_{R} \end{bmatrix}^{-1} \begin{pmatrix} P_{\Lambda}^{\text{meas}} \\ P_{\Lambda}^{\text{meas}} \end{pmatrix} \end{split}$$

Becattir

$$\begin{pmatrix} \varpi_{c} \\ B_{c}/T \end{pmatrix} = \begin{bmatrix} \frac{2}{3} \sum_{R} \left(f_{\Lambda R} C_{\Lambda R} - \frac{1}{3} f_{\Sigma^{0} R} C_{\Sigma^{0} R} \right) S_{R}(S_{R} + 1) & \frac{2}{3} \sum_{R} \left(f_{\Lambda R} C_{\Lambda R} - \frac{1}{3} f_{\Sigma^{0} R} C_{\Sigma^{0} R} \right) (S_{R} + 1) \mu_{R} \\ \frac{2}{3} \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) & \frac{2}{3} \sum_{\overline{R}} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) (S_{\overline{R}} + 1) \mu_{\overline{R}} \end{bmatrix}^{-1} \begin{pmatrix} P_{\Lambda}^{\text{meas}} \\ P_{\overline{\Lambda}}^{\text{meas}} \\ P_{\overline{\Lambda}}^{\text{meas}} \end{pmatrix} = \begin{bmatrix} 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{R}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1) \\ 2 \sum_{R} \left(f_{\overline{\Lambda R}} C_{\overline{\Lambda R}} - \frac{1}{3} f_{\overline{\Sigma}^{0} \overline{R}} C_{\overline{\Sigma}^{0} \overline{R}} \right) S_{\overline{R}}(S_{\overline{R}} + 1)$$

Decay	С
Parity conserving: $1/2^+ \rightarrow 1/2^+ 0^-$	-1/3
Parity conserving: $1/2^- \rightarrow 1/2^+ 0^-$	1
Parity conserving: $3/2^+ \rightarrow 1/2^+ 0^-$	1/3
Parity-conserving: $3/2^- \rightarrow 1/2^+ 0^-$	-1/5
$\Xi^0 ightarrow \Lambda + \pi^0$	+0.900
$\Xi^- ightarrow \Lambda + \pi^-$	+0.927
$\frac{\Sigma^0 \to \Lambda + \gamma}{}$	-1/3

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$^{\rm D}$ Only ~25% of measured Λ and anti- Λ are primary, while ~60% are feed-down

15%-20% dilution of primary Λ polarization (model-dependent)

nt R to Λ



More precise measurement at $\sqrt{s_{NN}} = 200$ *GeV*



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Confirmed energy dependence of P_H with new results for 200 GeV - $>5\sigma$ significance utilizing 1.5B events (2010+2011+2014) - partly due to stronger shear flow structure in lower $\sqrt{s_{NN}}$ because of baryon stopping

- Theoretical models can describe the data well

I. Karpenko and F. Becattini, EPJC(2017)77:213, UrQMD+vHLLE H. Li et al., PRC96, 054908 (2017), AMPT Y. Sun and C.-M. Ko, PRC96, 024906 (2017), CKE Y. Xie et al., PRC95, 031901(R) (2017), PICR D.-X. Wei et al., PRC99, 014905 (2019), AMPT

- $P_H(\Lambda)$ [%] = 0.277 ± 0.040(stat) ±^{0.039}_{0.049} (sys)
- $P_H(\bar{\Lambda})$ [%] = 0.240 ± 0.045(stat) ±^{0.061}_{0.045} (sys)





How about at higher/lower energy?



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- **ALICE** preliminary Pb+Pb at $\sqrt{s_{NN}} = 2.76$ TeV
 - $P_H(\Lambda)[\%] = -0.08 \pm 0.10 \text{ (stat)} \pm 0.04 \text{ (syst)}$ $P_H(\bar{\Lambda})[\%] = 0.05 \pm 0.10 \text{ (stat)} \pm 0.03 \text{ (syst)}$
 - M. Konyushikhin, QCD Chirality Workshop 2017
 - **HADES** preliminary Au+Au at $\sqrt{s_{NN}} = 2.4$ GeV -
 - $P_H(\Lambda)[\%] = 3.672 \pm 0.699 \text{ (stat.)}$ $P_H^{\rm BG}[\%] = 3.689 \pm 1.133 \text{ (stat.)}$
 - F. Kornas, SQM2019





Centrality dependence of P_H



In most central collision \rightarrow no initial angular momentum As expected, the polarization decreases in more central collisions

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A polarization vs. charge asymmetry



$$\mu_{\rm v}/T \propto \frac{\langle N_+ - N_- \rangle}{\langle N_+ + N_- \rangle} = A_{\rm ch} \qquad \qquad \begin{array}{c} \text{B-field } \mathbf{p} & \text{sp} \\ \uparrow & \uparrow & \uparrow \\ \mu_{\rm v} > 0 & \downarrow \\ \downarrow \text{LH} & \downarrow \\ \end{array}$$

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Local vorticity

vortex induced by jet



YT and T. Hirano, Nucl.Phys.A904-905 2013 (2013) 1023c-1026c Y. Tachibana and T. Hirano, NPA904-905 (2013) 1023 B. Betz, M. Gyulassy, and G. Torrieri, PRC76.044901 (2007)

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local vorticity induced by collective flow



L.-G. Pang, H. Peterson, Q. Wang, and X.-N. Wang, PRL117, 192301 (2016) F. Becattini and I. Karpenko, PRL120.012302 (2018) S. Voloshin, EPJ Web Conf.171, 07002 (2018)





Polarization along the beam direction

S. Voloshin, SQM2017

F. Becattini and I. Karpenko, PRL120.012302 (2018)





Stronger flow in in-plane than in out-of-plane could make local polarization along beam axis!

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Polarization along the beam direction



- Effect of Ψ_2 resolution is not corrected here

C Valachin CON17017

F. Becattini and I. Karpenko, PRI 120012302 (2018)



- Y. Sun and C.-M. Ko, PRC99, 011903(R) (2019) - Y. Xie, D. Wang, and L. P. Csernai, arXiv:1907.00773











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).9





Dew data of 27 GeV and BESII for 7.7-19.6 GeV (collider) and 3-7.7 GeV (fixed target)





Summary

^D CME/CVE

- A lot of studies with various observables are ongoing but no definitive conclusion so far
- Good progress to quantify possible CME contributions to the measurements
- Stay tuned for isobaric data
- \square Λ global polarization
 - Experimental evidence of the most vortical fluid

 - HADES result indicates the polarization decreases around $\sqrt{s_{NN}} = 2.4 7.7$ GeV → BES II STAR-FXT $\sqrt{s_{NN}} = 3-7.7$ GeV
- \Box First study of Λ polarization along the beam direction at $\sqrt{s_{NN}} = 200$ GeV
 - Quadrupole structure of the polarization relative to the 2nd-order event plane \rightarrow consistent with a picture of the elliptic flow but agree/disagree among the data and theoretical calculations in the sign

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• Polarization increases in lower energies within $\sqrt{s_{NN}} = 7.7-200$ GeV, consistent with theoretical models



Back up

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Signal extraction with A hyperons



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βμ 1 βm *Effect of non-zero chemical potential*



Non-zero chemical potential makes polarization splitting between Λ and anti- Λ , but the effect seems to be small.

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Y. Karpenko, sQM2017

 Λ and $\overline{\Lambda}$: UrQMD+vHLLE vs experiment





only $\mu_{\rm B}$ effect in model



Vorticity in HIC



In non-central collisions, the initial collective longitudinal flow velocity depends on x.

$$\omega_y = \frac{1}{2} (\nabla \times v)_y \approx -\frac{1}{2} \frac{\partial v_z}{\partial x}$$

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Possible probe of magnetic field



Becattini, Karpenko, Lisa, Upsal, and Voloshin, PRC95.054902 (2017)

$$P_{\Lambda} \simeq \frac{1}{2} \frac{\omega}{T} + \frac{\mu_{\Lambda} B}{T}$$

$$P_{\overline{\Lambda}} \simeq \frac{1}{2} \frac{\omega}{T} - \frac{\mu_{\Lambda} B}{T}$$

$$\mu_{\Lambda:} \Lambda \text{ magnetic moment}$$

$$B = (P_{\Lambda} - P_{\overline{\Lambda}}) k_B T / \mu_{N}$$

$$\sim 5.0 \times 10^{13} \text{ [Tesla]}$$

nuclear magneton $\mu_N = -0.613 \mu_{\Lambda}$

McLerran and Skokov, Nucl. Phys. A929, 184 (2014)



Extracted B-field is close to our expectation. Need more data with better precision →BES-II and Isobaric collisions



Contributions to P_z in hydro

I. Karpenko, QM2018

Longitudinal quadrupole f_2 :





 P_z dominated by temperature gradient and relativistic term, but not by kinematic vorticity based on the hydro model.

Can we get such a small kinetic vorticity in the blast-wave









































Variations of model parameters for P_H





Initial state: R_{\perp} : transverse granularity R_n : longitudinal granularity

Fluid phase: η/s : shear viscosity of fluid

Particlization criterion: $\varepsilon_{sw} = 0.5 \text{ GeV/fm}^3$

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• Collision energy dependence is robust with respect to variation of the parameters of the model. • There is no big difference between event-by-event and single shot hydrodynamic description.





Sine modulation of ω_z is expected with the factor [b_n-a_n]. The sign could be negative depending on the relation of flow and spatial anisotropy.

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e blast-wave model

S. Voloshin, SQM2017 EPJ Web Conf.171, 07002 (2018)

 $r_{max} = R[1 - a\cos(2\phi_s)],$ $\rho_t = \rho_{t,max}[r/r_{max}(\phi_s)][1 + b\cos(2\phi_s)] \approx \rho_{t,max}(r/R)[1 + (a+b)\cos(2\phi_s)].$

Approximation of the kinetic vorticity in the blast-wave model:

 $\omega_z = 1/2(\nabla \times \mathbf{v})_z \approx (\rho_{t,nmax}/R) \sin(n\phi_s)[b_n - a_n].$

an: spatial anisotropy R: reference source radius b_n: flow anisotropy ρ_t: transverse flow velocity







Blast-wave model parameterization

- Hydro-inspired model parameterized with freeze-out condition assuming the longitudinal boost invariance
 - Freeze-out temperature T_f
 - Radial flow rapidity ρ_0 and its modulation ρ_2 —
 - Source size R_x and R_y

$$\rho(r,\phi_s) = \tilde{r}[\rho_0 + \rho_2 \cos(2\phi_b)]$$
$$\tilde{r}(r,\phi_s) = \sqrt{(r\cos\phi_s)^2/R_x^2 + (r\sin\phi_s)^2}$$

Calculate vorticity at the freeze-out using the parameters • extracted from spectra, v₂, and HBT fit

$$\langle \omega_z \sin(2\phi) \rangle = \frac{\int d\phi_s \int r dr \, I_2(\alpha_t) K_1(\beta_t) \omega_z \sin(2\phi_b)}{\int d\phi_s \int r dr \, I_0(\alpha_t) K_1(\beta_t)}$$
$$\omega_z = \frac{1}{2} \left(\frac{\partial u_y}{\partial x} - \frac{\partial u_x}{\partial y} \right),$$

u: local flow velocity, In, Kn: modified Bessel functions

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 $(s)^2/R_u^2$





 ϕ_s : azimuthal angle of the source element ϕ_b : boost angle perpendicular to the elliptical subshell







Disagreement in P_z sign

Opposite sign

- UrQMD (or Glauber) IC + hydrodynamic model
 - F. Becattini and I. Karpenko, PRL.120.012302 (2018)
 - -- Assuming a local thermal equilibrium
- AMPT
- X. Xia, H. Li, Z. Tang, Q. Wang, PRC98.024905 (2018)

Same sign

- Chiral kinetic approach
 - Y. Sun and C.-M. Ko, PRC99, 011903(R) (2019)
 - -- Assuming non-equilibrium of spin degree of freedom
- PICR hydrodynamic model
 - Y. Xie, D. Wang, and L. P. Csernai, arXiv:1907.00773
 - Yang-Mills flux tube IC

Incomplete thermal equilibrium of spin degree of freedom? In hydrodynamic model, importance of relativistic contribution (from expansion and temporal term) in addition to kinematic vorticity.

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P_z modulation from the BW model

BW parameters obtained with HBT: STAR, PRC71.044906 (2005)



Simple estimate for kinematic vorticity contribution with BW model T. Niida, S. Voloshin, A. Dobrin, and R. Bertens, in preparation

- Similar magnitude to the data
- Inclusion of HBT in the fit affects the sign in peripheral collisions \bullet

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STAR, arXiv:1905.11917





